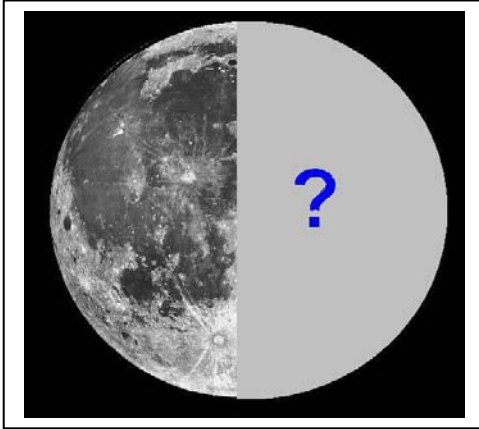


# The Moon's Density - What's inside?



The Moon has a mass of  $7.4 \times 10^{22}$  kilograms and a radius of 1,737 kilometers. Seismic data from the Apollo seismometers also shows that there is a boundary inside the Moon at a radius of about 400 kilometers where the rock density or composition changes. Astronomers can use this information to create a model of the Moon's interior.

Problem 1 - What is the average density of the Moon in grams per cubic centimeter ( $\text{g/cm}^3$ ) ? (Assume the Moon is a perfect sphere.)

Problem 2 - What is the volume, in cubic centimeters, of A) the Moon's interior out to a radius of 400 km? and B) The remaining volume out to the surface?

You can make a simple model of a planet's interior by thinking of it as an inner sphere (the core) with a radius of  $R(\text{core})$ , surrounded by a spherical shell (the mantle) that extends from  $R(\text{core})$  to the planet's surface,  $R(\text{surface})$ . We know the total mass of the planet, and its radius,  $R(\text{surface})$ . The challenge is to come up with densities for the core and mantle and  $R(\text{core})$  that give the total mass that is observed.

Problem 3 - From this information, what is the total mass of the planet model in terms of the densities of the two rock types ( $D_1$  and  $D_2$ ) and the radius of the core and mantle regions  $R(\text{core})$  and  $R(\text{surface})$ ?

Problem 4 - The densities of various rock types are given in the table below.

Type	Density
I - Iron+Nickle mixture (Earth's core)	15.0 gm/cc
E - Earth's mantle rock (compressed)	4.5 gm/cc
B - Basalts	2.9 gm/cc
G - Granite	2.7 gm/cc
S - Sandstone	2.5 gm/cc

A) How many possible lunar models are there? B) List them using the code letters in the above table, C) If denser rocks are typically found deep inside a planet, which possibilities survive? D) Find combinations of the above rock types for the core and mantle regions of the lunar interior model, that give approximately the correct lunar mass of  $7.4 \times 10^{25}$  grams. [Hint: use an Excel spread sheet to make the calculations faster as you change the parameters.] E) If Apollo rock samples give an average surface density of 3.0 gm/cc, which models give the best estimates for the Moon's interior structure?

**Problem 1** - Mass =  $7.4 \times 10^{22}$  kg x 1000 gm/kg =  $7.4 \times 10^{25}$  grams. Radius = 1,737 km x 100,000 cm/km =  $1.737 \times 10^8$  cm. Volume of a sphere =  $\frac{4}{3} \pi R^3 = \frac{4}{3} \times (3.141) \times (1.737 \times 10^8)^3 = 2.2 \times 10^{25} \text{ cm}^3$ , so the density =  $7.4 \times 10^{25} \text{ grams} / 2.2 \times 10^{25} \text{ cm}^3 = 3.4 \text{ gm} / \text{cm}^3$ .

**Problem 2** - A)  $V(\text{core}) = \frac{4}{3} \pi R^3 = \frac{4}{3} \times (3.141) \times (4.0 \times 10^7)^3 = 2.7 \times 10^{23} \text{ cm}^3$   
 B)  $V(\text{shell}) = V(R_{\text{surface}}) - V(R_{\text{core}}) = 2.2 \times 10^{25} \text{ cm}^3 - 2.7 \times 10^{23} \text{ cm}^3 = 2.17 \times 10^{25} \text{ cm}^3$

**Problem 3** - The total core mass is given by  $M(\text{core}) = \frac{4}{3} \pi (R_{\text{core}})^3 \times D_1$ . The volume of the mantle shell is given by multiplying the shell volume  $V(\text{shell})$  calculated in Problem 2B by the density:  $M_{\text{shell}} = V(\text{shell}) \times D_2$ . Then, the formula for the total mass of the model is given by:  $MT = \frac{4}{3} \pi (R_c)^3 \times D_1 + (\frac{4}{3} \pi (R_s)^3 - \frac{4}{3} \pi (R_c)^3) \times D_2$ , which can be simplified to:

$$MT = \frac{4}{3} \pi (D_1 \times R_c^3 + D_2 \times R_s^3 - D_2 \times R_c^3)$$

**Problem 4** - A) There are 5 types of rock for 2 lunar regions so the number of unique models is  $5 \times 5 = 25$  possible models. B) The possibilities are: II, IE, IB, IG, IS, EE, EI, EB, EG, ES, BI, BE, BB, BG, BS, GI, GE, GB, GG, GS, SI, SE, SB, SG, SS. C) The ones that are physically reasonable are: IE, IB, IG, IS, EB, EG, ES, BG, BS, GS. The models, II, EE, BB, GG and SS are eliminated because the core must be denser than the mantle. D) Each possibility in your answer to Part C has to be evaluated by using the equation you derived in Problem 3. This can be done very efficiently by using an Excel spreadsheet. The possible answers are as follows:

Model Code	Mass (in units of $10^{25}$ grams)
I E	10.2
I B	6.7
E B	6.4
I G	6.3
E G	6.0
B G	6.0
I S	5.8
E S	5.5
B S	5.5
G S	5.5

E) The models that have rocks with a density near 3.0 gm/cc as the mantle top layer are the more consistent with the density of surface rocks, so these would be IB and EB which have mass estimates of  $6.7 \times 10^{25}$  and  $6.4 \times 10^{25}$  grams respectively. These are both very close to the actual moon mass of  $7.4 \times 10^{25}$  grams ( e.g.  $7.4 \times 10^{22}$  kilograms ) so it is likely that the moon has an outer mantle consisting of basaltic rock, similar to Earth's mantle rock (4.5 gm/cc) and a core consisting of a denser iron/nickel mixture (15 gm/cc).